

# Viscosity Measurements on Carbon Monoxide, Nitrogen up to 900 Atmospheres and Correlation to Mass Diffusion

GIAN LUIGI CHIERICI

Servizio Geochimico, AGIP-Direzione Mineraria, Milano (Italy)

and ALBERTO PARATELLA

Istituto di Impianti Chimici dell'Università di Padova (Italy)

TABLE I. VISCOSITY VALUES CALCULATED BY THE DILUTE GAS THEORY (4)

$P = 1 \text{ atm.}; T = 323.1^\circ\text{K.}$	$A = \text{CO}$	$B = \text{N}_2$	$\text{CO}\cdot\text{N}_2$
Collision integral (7)	0.989	0.998	0.9925
Molecular diameter, Å. (7)	3.706	3.681	3.693
Viscosity, $10^6$ poise	187.0	187.8	187.6

At high pressures the viscosity of gaseous mixtures can be measured with great accuracy. For this reason, viscosity data can offer a profitable means of checking other transport properties of the mixture, such as mass diffusivity, which are difficult to measure accurately.

The present paper is aimed to check the experimental mass diffusivity data for the carbon monoxide-nitrogen mixture, which have been obtained by the dynamic method up to 600 atm. (1, 2). The application of this method at high pressure is relatively recent; it presents some advantages with respect to the discontinuous method but also some operational difficulties. Thus, a check of the results was needed. To this aim, viscosity measurements have been carried out on the same mixture and the correlation between viscosity and mass diffusivity has been derived by Enskog's theory. The carbon monoxide-nitrogen mixture has been chosen, because the molecular parameters of its components are very similar so that the correlation between the two transport properties approximates that given by Enskog for single gases.

## CORRELATION BETWEEN VISCOSITY AND MASS DIFFUSIVITY

In the mixture of components A and B, the binary coefficient of mass diffusion  $D_{AB}$ , at pressure  $P$  can be expressed by:

$$D_{AB} = (D_{AB})_1 \frac{Z}{P X_{AB}} \quad (1)$$

$Z$  is the compressibility factor of the mixture.  $X_{AB}$  is a function of  $P$ , depending on the diameters of molecules A and B (3).  $(D_{AB})_1$  denotes the diffusion coefficient calculated at  $P = 1$  atm. by the dilute gas theory, at the same temperature of  $D_{AB}$ .

In turn,  $(D_{AB})_1$  is related to the interaction term,  $(\eta_{AB})_1$  (5), which appears in the equation for the mixture viscosity,  $(\eta_m)_1$ :

$$(\eta_m)_1 = (\eta_m)_1 (\eta_A, \eta_B, \eta_{AB}, x_A, x_B)_1 \quad (2)$$

As in Equation (1), index 1 refers to the state at  $P = 1$  atm.,  $(\eta_A)_1$  and  $(\eta_B)_1$  being the viscosities of the single components (5) and  $x_A, x_B$  the mole fractions.

For the mixture of A = carbon monoxide and B = nitrogen at temperature  $T = 323, 1^\circ\text{K.}$  of our measurements, Equation (2) in the form given by Waldmann (6) leads to:

$$\left( \frac{d(\eta_m)_1}{dx_B} \right)_{x_A \rightarrow 1} = 1.998 [(\eta_{AB})_1 - (\eta_A)_1];$$

$$\left( \frac{d(\eta_m)_1}{dx_B} \right)_{x_B \rightarrow 1} = 2.000 [(\eta_B)_1 - (\eta_{AB})_1] \quad (3)$$

Table I also shows that  $(\eta_A)_1 < (\eta_{AB})_1 < (\eta_B)_1$  and that  $(\eta_A)_1 \cong (\eta_B)_1$ . According to Equation (3), the interaction term,  $(\eta_{AB})_1$ , can be simply determined by:

$$(\eta_{AB})_1 \cong \frac{(\eta_A)_1 + (\eta_B)_1}{2} \quad (4)$$

At high pressures, a correlation of type (2) is no longer available but we find that the linear dependence of  $\eta_m$  on the mixture composition is substantially fulfilled, with  $\eta_A \cong \eta_B$ . Hence, the term  $\eta_{AB}$  can still be determined from the experimental values  $\eta_A, \eta_B$  by an equation of type (4), while the calculation can be carried out by an equation which approximates that given by Enskog for the viscosity of single gases (8):

$$\eta_i = (\eta_i)_1 \left[ \frac{1}{X_i} + 0.800 \left( \frac{b_0}{\bar{V}_i} \right) + 0.761 \left( \frac{b_0}{\bar{V}_i} \right)^2 X_i \right]$$

$$i = A; B \quad (5)$$

In Equation (5),  $b_{0i}$  and  $\bar{V}_i$  are the second virial coefficient and the molar volume, respectively, of component  $i$ . The term  $X_i$  is analogous to  $X_{AB}$  of Equation (1).

By putting  $i = AB$  in Equation (5), combination of Equations (1) and (5) gives:

$$\eta_{AB} \cong \frac{P}{\alpha TZ} \left[ D_{AB} + 0.800 \frac{b_0(D_{AB})_1}{RT} + 0.761 \left( \frac{b_0(D_{AB})_1}{RT} \right)^2 \frac{1}{D_{AB}} \right] \quad (6)$$

$$\alpha = 3.52 \frac{\Omega_d}{\Omega_v} \quad (7)$$

where  $\Omega_d, \Omega_v$  denote the generalized collision integrals for mass diffusivity and for viscosity, respectively, of the pair AB.

When  $P \rightarrow 1$ , one can recognize in Equation (6) the correlation between viscosity and mass diffusivity as given by Chapman-Enskog (9). When  $P$  increases, the decreasing of  $D_{AB}$  makes the last term in square brackets more and more important until finally it predominates. In this case Equation (6) predicts an inverse proportionality between viscosity and mass diffusivity as for liquids.

In order to apply Equation (6), specification of  $b_0$  is needed. To this aim, we consider the virial coefficients of the components carbon monoxide and nitrogen and we compare them, after checking how the original formulation of such terms is modified at high pressures.

## THE INTERMEDIATE AND HIGH PRESSURE REGIONS

Each of these regions corresponds to a different definition of the terms  $b_{0i}$  and  $X_i$ , which appear in Equations (5) and (6), the limit between the two regions depending upon the particular gas.

In the intermediate region, according to the original definition of  $X_i$ :

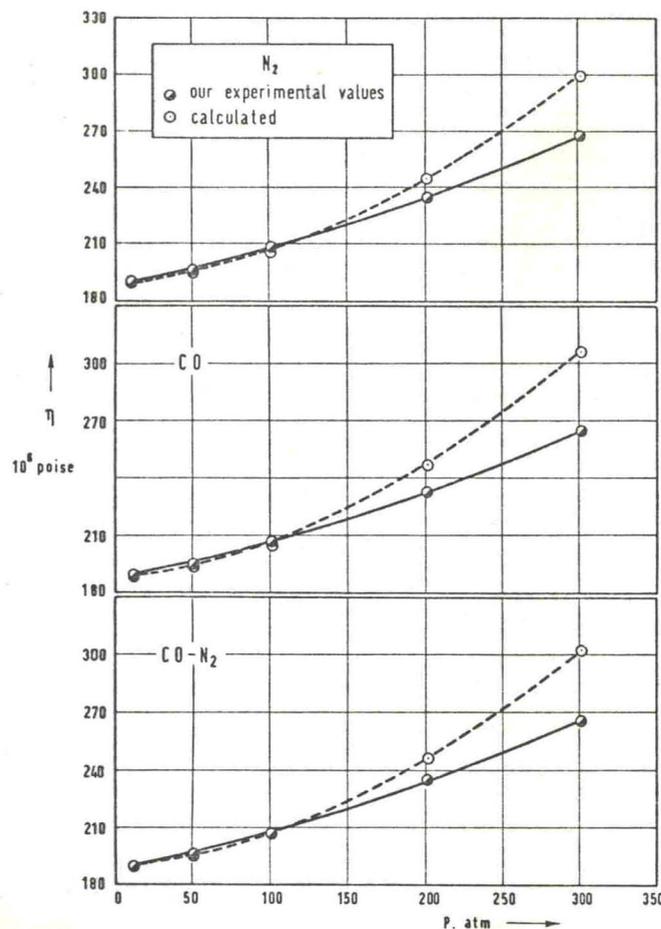


Fig. 1. Comparison between the experimental values of viscosity and those calculated by Equations (5), (9), and (10).

$$X_i = \frac{(P\bar{V}_i/RT) - 1}{(b_0/\bar{V}_i)} \quad (8)$$

the following equations are available (10):

$$X_i = 1 + 0.625 \left( \frac{b_0}{\bar{V}} \right)_i + 0.2869 \left( \frac{b_0}{\bar{V}} \right)_i^2 + 0.115 \left( \frac{b_0}{\bar{V}} \right)_i^3 \quad (9)$$

$$\left( \frac{b_0}{\bar{V}} \right)_i = \frac{2}{3} \pi n_i \sigma_i^3 \quad (10)$$

$n_i$  indicates the concentration of molecules  $i$ , having diameter  $\sigma_i$ .

By Equations (5), (9), (10) the viscosity of carbon monoxide and nitrogen has been calculated, utilizing the molar volume figures obtained by our P.V.T. data (see Table 3). Figure 1 shows that the agreement between

TABLE 2. EXPERIMENTAL VISCOSITIES OF CARBON MONOXIDE AND OF NITROGEN AT 50.0°C.

P Int'l. atm.	CO	Viscosity, 10 <sup>6</sup> poise N <sub>2</sub>	CO·N <sub>2</sub> Equation (4)
6	186.7	187.0	186.86
11	188.6	190.3	189.55
51	195.9	196.6	196.1
101	206.4	207.9	207.15
201	232.8	235.7	234.25
301	264.3	267.4	265.35

calculated and experimental values of viscosity is satisfactory only up to 200 atm., as concluded from earlier measurements at 298°K. (11).

Beyond 200 atm., which appears to be the upper limit of the intermediate pressure region for both carbon monoxide and nitrogen, Equations (8) and (10) have been modified, substituting pressure  $P$  by the total pressure  $P_{\text{tot.}}$ , as given by (12):

$$P_{\text{tot.}} = T \left( \frac{\partial P}{\partial T} \right)_{\bar{V}} \quad (11)$$

and substituting virial coefficient  $b_{0i}$  by the pseudo-virial coefficient  $b_i$ , as given by (12):

$$b_i = \frac{1}{2.545} \left( \frac{\eta \bar{V}}{(\eta)_1} \right)_{i, \text{exp. min.}} \quad (12)$$

In Equation (12),  $(\eta \bar{V}/(\eta)_1)_{i, \text{exp. min.}}$ , indicating the minimum value of the term in brackets for a real gas, must be determined experimentally.

Thus,  $X_i$  becomes:

$$X_i = \frac{(\bar{V}_i/R) (\partial P/\partial T)_{\bar{V}_i} - 1}{(b/\bar{V})_i} \quad (13)$$

In order to check the above semiempirical formulae, P.V.T. measurements were carried out in the range from 293 to 373°K. With the experimental values of the compressibility factor,  $Z$ , (see Table 3) the slope  $(\partial P/\partial T)_{\bar{V}_i} = P/T + (P/Z) (\partial Z/\partial T)_{\bar{V}_i}$  has been graphically determined by the method of residuals (13). The term  $b_i$  has been obtained from the minimum of the experimental curves reported in Figure 2.

Table 4 shows that the viscosity values calculated by Equations (5), (12), (13) agree with the experimental ones and agreement appears to improve as the pressure increases. In particular, the values of  $b_i$  appear to be substantially equal for both carbon monoxide and nitrogen.

Table 4 confirms the reliability of Equations (5), (12), (13) for predicting the viscosity of carbon monoxide and nitrogen and the reliability of Equation (6) for correlating viscosity a mass diffusivity of the carbon monoxide-nitrogen mixture. In Figure 4 the continuous curve collects the val-

TABLE 3. COMPRESSIBILITY FACTOR,  $Z$ , OF CARBON MONOXIDE AND OF NITROGEN FROM OUR P.V.T. MEASUREMENTS

P int'l. atm.	CO (Purity 0.9995) Compressibility factor, $Z$ :					N <sub>2</sub> (Purity 0.9999) Compressibility factor, $Z$ :				
	0°C.	25°C.	50°C.	75°C.	100°C.	0°C.	25°C.	50°C.	75°C.	100°C.
1	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
51	0.978	0.991	0.9995	1.006	1.011	0.988	0.999	1.004	1.012	1.016
101	0.972	0.995	1.010	1.021	1.028	0.987	1.007	1.018	1.029	1.036
201	1.019	1.0435	1.062	1.0735	1.082	1.039	1.060	1.077	1.085	1.092
301	1.119	1.133	1.143	1.151	1.155	1.137	1.149	1.159	1.162	1.165
401	1.246	1.245	1.244	1.243	1.241	1.260	1.258	1.257	1.253	1.250
501	1.3825	1.364	1.354	1.342	1.332	1.395	1.3795	1.367	1.3515	1.341
601	1.5225	1.430	1.469	1.448	1.430	1.529	1.499	1.477	1.4535	1.435
701	1.661	1.620	1.585	1.553	1.529	1.665	1.6215	1.590	1.558	1.532
801	1.802	1.747	1.703	1.662	1.628	1.803	1.747	1.7035	1.6625	1.629
901	1.940	1.872	1.816	1.768	1.7265	1.936	1.8695	1.816	1.7675	1.726

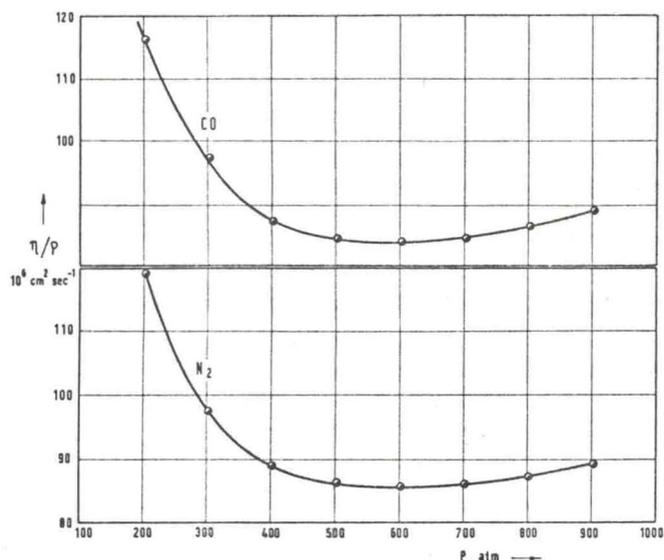


Fig. 2. Experimental values of momentum diffusivity,  $\eta/\rho$ .

TABLE 4. COMPARISON BETWEEN OUR EXPERIMENTAL DATA AND THOSE CALCULATED BY EQUATIONS (5), (12), (13)

P int'l. atm	N <sub>2</sub> at 50°C.			CO at 50°C.				
	$\frac{P_{tot.} \bar{V}_i}{RT} - 1$	$\left(\frac{b}{\bar{V}}\right)_i$	$\eta, 10^6$ poise	$\frac{P_{tot.} \bar{V}_i}{RT} - 1$	$\left(\frac{b}{\bar{V}}\right)_i$	$\eta, 10^6$ poise		
			calc.	exp.		calc.	exp.	
201	0.4644	0.3535	219.6	235.7	0.4265	0.3544	230.0	232.8
301	0.6819	0.4919	257.4	267.4	0.6660	0.4931	258.9	264.3
401	0.8702	0.6044	296.5	300.0	0.8671	0.6034	294.8	296.9
501	1.0382	0.6944	333.0	334.7	1.0451	0.6925	330.5	330.9
601	1.1875	0.7708	368.7	368.8	1.2112	0.7659	364.8	364.3
701	1.3459	0.8350	402.6	401.3	1.3734	0.8278	398.3	399.0
801	1.5008	0.8907	436.3	434.0	1.5287	0.8805	430.9	430.0
901	1.6460	0.9398	469.5	467.7	1.6878	0.9286	464.8	467.4

ues of the binary diffusion coefficient,  $D_{CO, N_2}$ , calculated with Equations (6) and (12) by our viscosity measurements. The circles indicate our experimental values of  $D_{CO, N_2}$  previously measured at the same temperature by the dynamic method (2).

## EXPERIMENTAL

### Equipment

A viscometer has been built by the Servizio Geochimico, AGIP—Direzione Mineraria, Milano, which satisfactorily compromises accurate measurement and simple operation. Figure 3 shows the main elements: reservoirs a and b, gas capillary c and mercury tube d. These are connected forming a rigid parallelogram, in which mercury and a known quantity of the gas are confined. By automatic control the rigid parallelogram can rotate around point O to assume four inclinations (see Table 5), allowing as many viscosity measurements at the same pressure.

The gas volume forced through the capillary during one run is determined by timing the motion of the mercury level between the two contacts  $e_1$  and  $e_2$ .

TABLE 5. CHARACTERISTICS OF THE VISCOMETER. INDEX 0 REFERS TO ZERO VALUE OF THE INCLINATION ANGLE,  $\theta$ , (SEE FIGURE 3)

$S_0 = 4.909$ sq. cm. $e_0 = 1.486$ cm. $V = V_0 = 7.295$ cc.					
Inclination	cos $\theta$	$S = S_0/\cos \theta$		$h_1$ cm.	$h_2$ cm.
		sq. cm.	cm.		
1	0.9976	4.921	1.482	6.312	3.348
2	0.9934	4.942	1.476	10.464	7.512
3	0.9641	5.092	1.432	24.179	21.315
4	0.9062	5.417	1.347	38.525	35.831

### Instrument Equation

The instrument equation has been provided because of the difference in construction and operation characteristics between our instrument and other similar devices [that is Eakin's jointed parallelogram device (14)].

A preliminary analysis proves the friction losses of laminar flow negligible in comparison to that at the inlet length of the gas capillary which caused by the initial acceleration of the fluid and the change of the velocity profile from a uniform to a parabolic distribution (15).

Since the gas capillary and the mercury tube are conical at both ends (cone angle = 1/20), it can be assumed that the entrance and the exit energy losses compensate each other under adiabatic flow conditions.

Thus, neglecting the change in the specific volume of the gas during its displacement, the motion can be described by:

$$\text{mercury } \Delta P = -\rho_{Hg}gh + \frac{8\eta_{Hg}v_{Hg}L_{Hg}}{r^2_{Hg}}$$

$$\text{gas } -\Delta P = \rho gh + \frac{8\eta v L}{r^2} + \beta v^2 \quad (14)$$

$\Delta P$  denotes the pressure drop corresponding to the height difference,  $h$ , (see Figure 3) between the interfaces mercury-gas in reservoirs a and b,  $\rho$  and  $v$  indicate the density and the mean velocity of the gas through the capillary of length  $L$ ;  $\rho_{Hg}$  and  $v_{Hg}$  are the corresponding quantities for the mercury displaced through the tube of length  $L_{Hg}$ . The term  $\beta v^2$  represents after Langhaar (16) the friction loss at the inlet length of the capillary, being  $\beta$  a dimensionless factor which can vary from 1.11 to 1.18 (17).

One introduces into Equations (14) the equality between the volume flow rates of the gas and of the mercury:

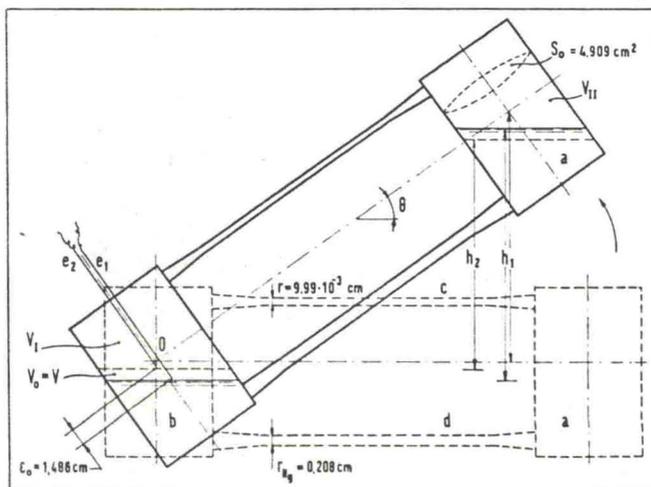


Fig. 3. Layout of the viscometer for measurements up to 1,500 atm.

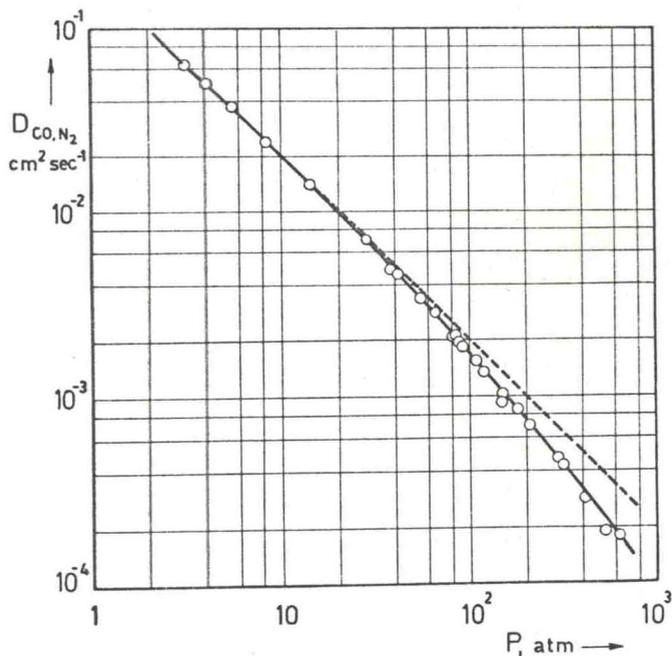


Fig. 4. Mass diffusivity,  $D_{CO, N_2}$ , calculated by experimental viscosity data with Equation (6) (continuous curve). The circles refer to experimental mass diffusivity values (2).

$$q = q_{Hg} = -\frac{S}{2} \frac{dh}{dt} \quad (15)$$

with  $t$  = time and  $S = S_0/\cos\theta$ .  $S$  is the instantaneous area of the interface mercury-gas (see Figure 3). By combining Equations (14) and (15) we get:

$$a \frac{S^2}{4} \left( \frac{dh}{dt} \right)^2 - \frac{S}{2} (d + d_{Hg}) \left( \frac{dh}{dt} \right) - ch = 0 \quad (16)$$

$$a = \frac{\beta \rho}{\pi^2 r^4}; \quad d = \frac{8\eta L}{\pi r^4}; \quad d_{Hg} = \frac{8\eta_{Hg} L_{Hg}}{\pi r^4_{Hg}}; \quad c = g(\rho_{Hg} - \rho) \quad (17)$$

Under the condition  $(dh/dt) < 0$ , the solution of Equation (16) is given by the negative root:

$$\frac{dh}{dt} \frac{d + d_{Hg}}{a S} [1 - (1 + \gamma h)^{1/2}] \quad (18)$$

$$\gamma = \frac{4 a c}{(d + d_{Hg})^2} \quad (19)$$

The integral of Equation (18) supplies time  $\bar{t}$  required for displacing the gas through the capillary:

$$\bar{t} = \frac{S(d + d_{Hg})}{4 a} \left\{ \ln \frac{h_2}{h_1} + 2[(1 + \gamma h_1)^{1/2} - (1 + \gamma h_2)^{1/2}] + \ln \frac{[(1 + \gamma h_2)^{1/2} + 1][(1 + \gamma h_1)^{1/2} - 1]}{[(1 + \gamma h_2)^{1/2} - 1][(1 + \gamma h_1)^{1/2} + 1]} \right\} \quad (20)$$

$h_1$  and  $h_2$  being the  $h$  values at the beginning and the end of the run, respectively.

In Equation (20) the terms  $S$ ,  $d_{Hg}$ ,  $h_1$  and  $h_2$  are known instrument constants.  $d$  and  $\gamma$  depend on the viscosity,  $\eta$ . By putting measured time  $\bar{t}$ , Equation (20) is iteratively solved until a satisfactory value of  $\eta$  is found.

Now, we verify the two main assumptions behind Equation (20). The first is that the gas flow through the capillary is laminar. Equations (14) and (15) have been combined and solved with respect to the gas velocity. This leads to the following expressions for the Reynolds number:

$$N_{Re} = \left[ \frac{64 r^6}{\beta^2} \left( \frac{L}{r^4} + \frac{\eta_{Hg} L_{Hg}}{\eta r^4_{Hg}} \right)^2 \right]$$

$$+ \frac{4 r^2 g}{\beta \eta^2} \rho h_1 (\rho_{Hg} - \rho) \left. \right]^{1/2} - \frac{8 r^3}{\beta} \left( \frac{L}{r^4} + \frac{\eta_{Hg} L_{Hg}}{\eta r^4_{Hg}} \right) \quad (21)$$

By Equation (21), the flow appears to be laminar when the instrument operates at the inclination 1 (see Table 5 and Figure 3). For the other inclinations it proved reliable to put into Equation (21) the value of  $t$  measured by the instrument at inclination 1 and to verify that the Reynolds number satisfies the condition  $N_{Re} \leq 1,500$ .

The second assumption behind Equation (20) is that the effective displaced volume of gas,  $V_{eff}$ , is equal to that  $V = \epsilon S$  of mercury. It implies that  $\Delta P \ll P$ . To this aim, we consider the instantaneous pressures,  $P_1^m$  and  $P_2^m$ , in reservoir b at the beginning and at the end of the run:

$$P_1^m = P + gh_1 (\rho_{Hg} - \rho) \frac{V_{II}}{(V_I + V) + V_{II}}; \quad P_2^m = P + gh_2 (\rho_{Hg} - \rho) \frac{V + V_{II}}{(V_I + V) + V_{II}} \quad (22)$$

$(V_I + V)$  and  $V_{II}$  indicate the gas volumes at the beginning of the run in reservoirs b and a, respectively. Since the mean pressure is  $P$ , the effective displaced volume of gas,  $V_{eff}$ , is given by:

$$V_{eff} P = (V_I + V) P_1^m + V_I P_2^m \quad (23)$$

By combining Equations (22) and (23), we get

$$\frac{V_{eff}}{V} = 1 + \frac{\delta}{P} \quad (24)$$

$$\delta = gh_1 (\rho_{Hg} - \rho) \frac{V_{II}(V_I + V) - V_I (V + V_{II}) (h_2/h_1)}{V(V + V_I + V_{II})} \quad (25)$$

the factor  $\delta$  varying from 0.1129 atm. at the first inclination to 0.2551 atm. at the last inclination of the instrument. By Equation (25), in the range  $P > 50$  atm., the ratio  $\delta/P$  becomes  $\leq 10^{-3}$  and the assumption  $V_{eff} \cong V$  is fulfilled. In the range  $P \leq 50$  atm., where the above assumption is satisfied only within some units percentage, Equation (20) has been corrected, by substituting the measured time,  $\bar{t}$ , with time  $t^*$  empirically formulated by:

$$t^* = \frac{\bar{t}}{1 + \delta/P} \quad (26)$$

Equation (26) derives from the fact that, when  $V_{eff}/V \leq 1.05$ , as is the case with  $P \leq 50$  atm., the time required for displacing the gas is linearly proportional to the effective displaced volume.

## CONCLUSION

In the pressure range up to 900 atm. our viscometer allows viscosity measurements with an accuracy 1%. Within this figure our data on nitrogen agree with those reported by Michels (18).

For the components carbon monoxide and nitrogen at 50°C., Enskog's theory satisfactorily predicts the behavior of the viscosity, whereas beyond 200 atm. is supplemented by P.V.T. measurements. The latter have been carried out with accuracy 1/1,000, which appears to be satisfactory for the present purpose.

The molecular similarity between carbon monoxide and nitrogen enables application of Enskog's theory in order to check the binary mass diffusivity data by those on viscosity.

## NOTATION

$b_0$ ;  $b$  = second virial coefficient for a hard spheres gas and for a real gas, respectively

$D_{AB}$  = binary coefficient of mass diffusion in the mixture of gases A and B  
 $g$  = gravity acceleration  
 $h$  = height difference between the interfaces mercury-gas in the viscometer reservoirs  
 $L; L_{Hg}$  = length of gas capillary and of mercury tube, respectively  
 $n$  = molecular concentration  
 $N_{Re}$  = Reynolds number  
 $P; P_{tot.}$  = experimental and total pressure of the gas, respectively  
 $\Delta P$  = pressure drop corresponding to height difference,  $h$   
 $q; q_{Hg}$  = volumetric flow rate of the gas and of the mercury, respectively  
 $r; r_{Hg}$  = radius of gas capillary and of mercury tube, respectively  
 $R$  = gas law constant  
 $S_0$  = area of the interface mercury-gas at zero inclination of the viscometer  
 $S$  = area of the interface mercury-gas in the viscometer reservoirs during a run  
 $\bar{t}; t^*$  = time required for displacing the mercury and the gas during a run, respectively.  $\bar{t} = t^*$  when  $P \cong 50$  atm.  
 $T$  = absolute temperature  
 $X_i$  = radial distribution function at distance  $\sigma_i$  from the center of a molecule  $i$  having diameter  $\sigma_i$   
 $V$  = volume between contacts  $e_1$  and  $e_2$  in reservoir b of the viscometer  
 $V + V_I$  = gas volume in reservoir b of the viscometer at the beginning of the run  
 $V_{II}$  = gas volume in reservoir a of the viscometer at the beginning of the run  
 $\bar{V}$  = molar volume  
 $Z$  = compressibility factor of the gas,  $Z = P\bar{V}/RT$

#### Greek Letters

$\epsilon_0$  = distance between contacts  $e_1$  and  $e_2$  in reservoir b at zero inclination of the viscometer  
 $\eta; \eta_{Hg}$  = viscosity of the gas and of the mercury, respectively  
 $\theta$  = inclination angle of the viscometer  
 $\rho; \rho_{Hg}$  = density of the gas and of the mercury, respectively  
 $\sigma_i$  = molecular diameter of specie  $i$  ( $i = A, B, AB$ )  
 $\Omega_d; \Omega_v$  = generalized collision integrals for mass diffusivity and for viscosity of molecular pair AB, respectively

$\delta$  = parameter, defined by Equations (24), (25), related to the volume change of the gas during its displacement through the capillary

#### Subscripts

$( )_1$  = for viscosity and for mass diffusivity at  $P = 1$  atm.  
 $i$  = for component  $i$  ( $i = A, B, AB$ )  
 $1; 2$  = for quantities at the beginning and at the end of a run, respectively  
 $eff$  = for effective displaced volume of gas through the capillary

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## Comparison of Lagrangian Time Correlations Obtained from Dispersion Experiments and from Space-Time Correlation Functions

J. M. RODRIGUEZ and G. K. PATTERSON

University of Missouri-Rolla, Rolla, Missouri

The relation between Lagrangian and Eulerian statistics for turbulent flow has been approached only through approximations or models of the actual motion. Some of these approaches have been motivated by a purely theoretical

interest in the problem (1 to 5) and others by need to justify the interpretation of an experimental measurement (6 to 10). Altogether, little progress has been made in this endeavor despite its importance in the research on tur-